



# IMPORTANT FORMULAE

## PROBABILITY Concepts and Formulae

Conditional Probability	Definition	<p>If E and F are two events associated with the same sample space of a random experiment, the conditional probability of the event E given that F has occurred, i.e. <math>P(E F)</math> is given by</p> $P(E F) = \frac{n(E \cap F)}{n(F)}$
	Properties	<p>E and F be events of a sample space S of an experiment</p> <ol style="list-style-type: none"> <li>1) <math>P(S F) = P(F F) = 1</math></li> <li>2) For any two events A and B of sample space S if F is another event such that <math>P(F) \neq 0</math>,  <math>P((A \cup B)   F) = P(A F) + P(B F) - P((A \cap B)   F)</math></li> <li>3) <math>P(E' F) = 1 - P(E F)</math></li> </ol>
Multiplication Theorem on Probability	For two events	<p>Let E and F be two events associated with a sample space S.</p> <p><math>P(E \cap F) = P(E) P(F E) = P(F) P(E F)</math> provided <math>P(E) \neq 0</math> and <math>P(F) \neq 0</math>.</p>
	For Three Events	<p>If E, F and G are three events of sample space S,</p> $P(E \cap F \cap G) = P(E) P(F E) P(G (E \cap F))$ $= P(E) P(F E) P(G EF)$
Independent Events	Definition	<ul style="list-style-type: none"> <li>▪ Let E and F be two events associated with the same random experiment Two events E and F are said to be independent, if             <ol style="list-style-type: none"> <li>(i) <math>P(F E) = P(F)</math> provided <math>P(E) \neq 0</math> and</li> <li>(ii) <math>P(E F) = P(E)</math> provided <math>P(F) \neq 0</math></li> <li>(iii) <math>P(E \cap F) = P(E) \cdot P(F)</math></li> </ol> </li> <li>▪ If E and F are independent events then so are             <ol style="list-style-type: none"> <li>(i) <math>E'</math> and F</li> <li>(ii) E and <math>F'</math></li> <li>(iii) <math>E'</math> and <math>F'</math></li> </ol> </li> </ul>
Bayes' Theorem	Partition of a sample space	<p>A set of events <math>E_1, E_2, \dots, E_n</math> is said to represent a partition of the sample space S if</p> <ol style="list-style-type: none"> <li>(a) <math>E_i \cap E_j = \phi, i \neq j, i, j = 1, 2, 3, \dots, n</math></li> <li>(b) <math>E_1 \cup E_2 \cup \dots \cup E_n = S</math></li> <li>(c) <math>P(E_i) &gt; 0</math> for all <math>i = 1, 2, \dots, n</math>.</li> </ol>



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	Theorem of Total probability	<p>Let <math>\{E_1, E_2, \dots, E_n\}</math> be a partition of the sample space <math>S</math>, and suppose that each of the events <math>E_1, E_2, \dots, E_n</math> has nonzero probability of occurrence. Let <math>A</math> be any event associated with <math>S</math>, then</p> $P(A) = P(E_1) P(A E_1) + P(E_2) P(A E_2) + \dots + P(E_n) P(A E_n)$ $= \sum_{j=1}^n P(E_j) P(A   E_j)$
	Bayes' Theorem	<p>If <math>E_1, E_2, \dots, E_n</math> are <math>n</math> non-empty events which constitute a partition of sample space <math>S</math> and <math>A</math> is any event of nonzero probability, then</p> $P(E_i   A) = \frac{P(E_i)P(A   E_i)}{\sum_{j=1}^n P(E_j)P(A   E_j)}$ for any $i = 1, 2, 3, \dots, n$
Random Variables and its Probability Distributions	Random Variable	A random variable is a real valued function whose domain is the sample space of a random experiment.
	Probability distribution of a random variable	<p>The probability distribution of a random variable <math>X</math> is the system of numbers</p> $X \quad : \quad x_1 \quad x_2 \quad \dots \quad x_n$ $P(X) \quad : \quad p_1 \quad p_2 \quad \dots \quad p_n$ <p>where <math>p_i &gt; 0, \sum_{i=1}^n p_i = 1, i = 1, 2, 3, \dots, n</math></p> <p>The real numbers <math>x_1, x_2, \dots, x_n</math> are the possible values of the random variable <math>X</math> and <math>p_i</math> (<math>i = 1, 2, \dots, n</math>) is the probability of the random variable <math>X</math> taking the value <math>x_i</math> i.e.</p> $P(X = x_i) = p_i$
	Mean of a random variable	<p>The mean of the random variable <math>X</math> is given by:</p> $\mu = \sum_{i=1}^n x_i p_i$ <p>The mean of a random variable <math>X</math> is also called the expectation of <math>X</math>, denoted by <math>E(X)</math>.</p> <p>Thus, <math>E(X) = \mu = \sum_{i=1}^n x_i p_i</math></p>
	Variance of a random variable	The variance of the random variable $X$ , denoted by $\text{Var}(X)$ or $\sigma_x^2$ is defined as



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		$\sigma_x^2 = \text{Var}(X) = \sum_{i=1}^n (x_i - \mu)^2 p(x_i) = E(X - \mu)^2$ $\text{Var}(X) = E(X^2) - [E(X)]^2$
	Standard Deviation	$\sigma_x = \sqrt{\text{Var}(X)} = \sqrt{\sum_{i=1}^n (x_i - \mu)^2 p(x_i)}$
Bernoulli Trials and Binomial Distribution	Bernoulli Trials	<p>Trials of a random experiment are called Bernoulli trials, if they satisfy the following conditions :</p> <ul style="list-style-type: none"> <li>(i) There should be a finite number of trials.</li> <li>(ii) The trials should be independent.</li> <li>(iii) Each trial has exactly two outcomes: success or failure.</li> <li>(iv) The probability of success remains the same in each trial.</li> </ul>
	Binomial distribution	<p>For Binomial distribution B (n, p),</p> $P(X = x) = {}^n C_x q^{n-x} p^x, x = 0, 1, \dots, n$ <p>(q = 1 - p)</p>