- (1) Find the area of the region bounded by the circle $x^2 + y^2 = r^2$. [Ans: πr^2]
- (2) Find the area of the region bounded by $y = x^2 5x + 4$ and X-axis.



(3) Find the area of the region enclosed by $y^2 = 8x$ and x + y = 0.

$$\left[\text{Ans}: \frac{32}{3} \right]$$

(4) Find the area of the region between the circles, $x^2 + y^2 = 4$ and $x^2 + y^2 = 4x$.

$$\left[\text{Ans:} \frac{8\pi}{3} - 2\sqrt{3} \right]$$

- (5) Prove that the area of the region bounded by $y = 4x x^2$ and X-axis is $\frac{32}{3}$.
- (6) Find the volume of the solid obtained by revolution of portion of the ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ on right hand semi-plane of Y-axis about Y-axis. $\left[\text{Ans}: \frac{4}{3} \pi a^2 b \right]$
- (7) If the region bounded by $y^2 = 8x$ from its vertex to x = 2 is rotated about X-axis, find the volume of the solid generated.

[Ans: 16 π]

(8) Prove that the volume of the solid generated by revolving the region bounded by $y = x^2 + 1$ and y = 2x + 1 about X-axis is $\frac{104 \pi}{15}$.



PROBLEMS

(9) Find the volume of the right circular cone having semi-vertical angle α and radius of base equal to r.

 $\left[\text{Ans}: \frac{1}{3}\pi r^3 \cot \alpha \right]$

(10) Line x = c divides the area of the region bounded by $y^2 = 4x$ and x = 16 in two regions having equal areas. Find c.

(11) Find the area of the region bounded by $y = x^2$ and the line y = x + 2.

 $\left[\text{Ans}: \frac{9}{2} \right]$

(12) Find the area of the region bounded by $y = 5x^2$ and $2x^2 - y + 9 = 0$.

[Ans: 12 √ 3]

(13) The region bounded by $y = 2x^2$, X-axis and x = 5 is rotated about Y-axis. Find the volume of the solid generated.

[Ans: 625 π]

(14) Find the volume of the solid generated when the region bounded by $y = x^2$ and $y = 4x - x^2$ is rotated about X-axis.

 $\left[\text{Ans}: \frac{32 \pi}{3} \right]$

(15) If the region bounded by $x^2 - y^2 = a^2$, x = a and x = 2a is rotated about Y-axis, find the volume of the solid of revolution.

[Ans: $4\sqrt{3}\pi a^3$]



PROBLEMS

- (16) Prove that the area of the region enclosed by the circle $x^2 + y^2 = 64$ and parabola $y^2 = 12x$ is $\frac{16}{3}(4\pi + \sqrt{3})$.
- (17) Prove that the area of the region bounded by $x = 6 + 4y y^2$ and \overrightarrow{AB} where A is (4, 3) and B is (-10, -4) is 36.
- (18) The region bounded by $y = 4x x^2$, x = 1, x = 3 and X-axis is divided into two parts with equal area by x = c. Find c.

[Ans: 2]

- (19) Obtain the area of the minor segment bounded by the circle $x^2 + y^2 = a^2$ and the line $x = \frac{a}{\sqrt{2}}$. $\left[\text{Ans: } \frac{a^2}{4} (\pi - 2) \right]$
- (20) Find the area of the region bounded by $y = x^2$ and y = 2 x.



(21) Obtain the area of the region bounded by the line through A(3, 2) and B(1, 1) and the curve $x = y^2 + y - 1$.

 $\left[\text{Ans}: \frac{1}{6} \right]$

(22) Obtain the area of the region bounded by the curve $y = x^2 + 1$ and the line passing through (0, 1) and (2, 5).



(23) Obtain the area of the region bounded by the curves $y^2 = 4x$ and $x^2 = 4y$.





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(24) Obtain the area of the region bounded between the circle $x^2 + y^2 = 4$ and the parabola $y^2 = 3x$.

 $\left[\text{Ans:} \frac{1}{3} (4\pi + \sqrt{3}) \right]$

- (25) Obtain the area of the region enclosed between the parabolas $y = 6x x^2$ and $y = x^2 2x$.
 - $\left[\text{Ans}: \frac{64}{3} \right]$
- (26) Obtain the volume of the solid surface generated on rotating the region bounded by the parabola $y = x^2$ and $y = 4x x^2$, about the X-axis.

 $\left[\text{Ans:} \frac{32 \pi}{3} \right]$

- (27) Show that the volume of the segment of a sphere with radius a between two parallel planes on one side of the centre at a distance r_1 and r_2 from the centre $(r_1 < r_2)$ is $\frac{\pi}{2}(r_2 r_1)[3a^2 (r_1^2 + r_1r_2 + r_2^2)].$
- (28) Obtain the area of the region enclosed between $y^2 = 4x 4$ and $y^2 = -4x + 4$.

$$\left[\text{Ans}: \frac{16}{3} \right]$$

(29) Obtain area of the region enclosed between the parabola $y^2 = 4(x - 2)$, the line y = x - 1 and the X-axis.

 $\left[\text{Ans}: \frac{2}{3} \right]$

(30) Find the volume of the solid generated on rotating the region bounded by the curve $y = x^2 + 1$ and the line y = 2x + 4, about the X-axis.

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\left[ \text{ Ans : } \frac{1408 \, \pi}{15} \right]
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(31) Find the volume of the solid generated on rotating the region bounded by $y^2 = x^3$, x = 2 and the X-axis about the X-axis.

[Ans: 4 π]

(32) Find the volume of the solid generated on rotating the region bounded by the curve $y = a\left(\sin x + \frac{\sin 3x}{3}\right)$, the X-axis and the lines x = 0 and $x = \pi$ about the X-axis. $\left[Ans: \frac{5\pi^2 a^2}{9}\right]$

(33) Find the common area enclosed between the ellipses $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ and $\frac{x^2}{b^2} + \frac{y^2}{a^2} = 1$ (a > b).

$$\left[\text{Ans: } 2ab\left(\pi - 2\sin^{-1}\frac{a}{\sqrt{a^2 + b^2}}\right) \right]$$

